

PHYSICS EXAMINATION PROBLEMS SOLUTIONS AND HINTS FOR STUDENT SELF-STUDY

Module Code	PHY2201
Name of module	Statistical Physics
Date of examination	Jan 2003

1. i) a) 8855,
b) broadens the energy levels (not covered in 2004 syllabus).
ii) $dp_i/dt = \sum_j v_{ij} (p_j - p_i)$ (NB this topic does not appear in the 2004) syllabus

2. i)
$$p_r = \frac{\exp(-\epsilon_r/k_B T)}{\sum_r \exp(-\epsilon_r/k_B T)}$$

$$\bar{\Omega} = \sum_r \Omega_r p_r = \frac{\sum_r \Omega_r \exp(-\epsilon_r/k_B T)}{\sum_r \exp(-\epsilon_r/k_B T)}$$

NB do not confuse the use of Ω in this question with its more usual use i.e. to represent the number of microstates compatible with a given macrostate.

- ii) a) they are equal (principle of equal probability for all accessible microstates)
b) macrostate B is more probable than A (higher entropy) as Ω (number of microstates compatible with that macrostate) is higher for B.
iii) thermal: max of entropy, as defined by Clausius's formula.
Statistical: max. of Ω i.e. evolution towards the most probable energy sharing configuration.
3. i) Use Clausius's defn of entropy change and relation between S, U, V and T given by FTR. Require that $dS_{\text{total}} > 0$ as change is irreversible. Hence show that $d'Q_A < 0$ if $T_A > T_B$. NB $d'Q$ means the inexact differential "d-bar Q ".
ii) Kelvin statement, from notes. Entropy cannot fall, easy to show it would if Kelvin statement violated.
iii) Use fact that $dS_{\text{total}} = \text{zero}$ if the process is perfectly reversible, which in turn implies greatest poss. efficiency.
4. a) Carnot cycle – see notes
b) ditto.
c) adiabatic: $dS = \text{zero}$. Isotherma $dS = \Delta Q/T$
d) Implied by 1st law and fact that U is a fn of state.
e) see notes. $\eta = 1 - T_2/T_1$ ($T_2 < T_1$)
5. i) see notes
ii) not covered in 2004 syllabus.